

## nag\_glm\_normal (g02gac)

### 1. Purpose

**nag\_glm\_normal (g02gac)** fits a generalized linear model with normal errors.

### 2. Specification

```
#include <nag.h>
#include <nagg02.h>

void nag_glm_normal(Nag_Link link, Nag_IncludeMean mean, Integer n,
  double x[], Integer tdx, Integer m, Integer sx[], Integer ip,
  double y[], double wt[], double offset[], double *scale,
  double ex_power, double *rss, double *df, double b[], Integer *rank,
  double se[], double cov[], double v[], Integer tdv, double tol,
  Integer max_iter, Integer print_iter, char *outfile, double eps,
  NagError *fail)
```

### 3. Description

A generalized linear model with Normal errors consists of the following elements:

- (a) a set of  $n$  observations,  $y_i$ , from a Normal distribution with probability density function:

$$\frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(y-\mu)^2}{2\sigma^2}\right),$$

where  $\mu$  is the mean and  $\sigma^2$  is the variance.

- (b)  $X$ , a set of  $p$  independent variables for each observation,  $x_1, x_2, \dots, x_p$ .  
 (c) a linear model:

$$\eta = \sum \beta_j x_j.$$

- (d) a link between the linear predictor,  $\eta$ , and the mean of the distribution,  $\mu$ , i.e.,  $\eta = g(\mu)$ . The possible link functions are:

- (i) exponent link:  $\eta = \mu^a$ , for a constant  $a$ ,
- (ii) identity link:  $\eta = \mu$ ,
- (iii) log link:  $\eta = \log \mu$ ,
- (iv) square root link:  $\eta = \sqrt{\mu}$ ,
- (v) reciprocal link:  $\eta = \frac{1}{\mu}$ .

- (e) a measure of fit, the residual sum of squares =  $\sum (y_i - \hat{\mu}_i)^2$

The linear parameters are estimated by iterative weighted least-squares. An adjusted dependent variable,  $z$ , is formed:

$$z = \eta + (y - \mu) \frac{d\eta}{d\mu}$$

and a working weight,  $w$ ,

$$w = \left(\frac{d\eta}{d\mu}\right)^2.$$

At each iteration an approximation to the estimate of  $\beta$ ,  $\hat{\beta}$ , is found by the weighted least-squares regression of  $z$  on  $X$  with weights  $w$ .

**nag\_glm\_normal** finds a  $QR$  decomposition of  $w^{\frac{1}{2}}X$ , i.e.,

$w^{\frac{1}{2}}X = QR$  where  $R$  is a  $p$  by  $p$  triangular matrix and  $Q$  is a  $n$  by  $p$  column orthogonal matrix.

If  $R$  is of full rank, then  $\hat{\beta}$  is the solution to:

$$R\hat{\beta} = Q^T w^{\frac{1}{2}} z$$

If  $R$  is not of full rank a solution is obtained by means of a singular value decomposition (SVD) of  $R$ .

$$R = Q_* \begin{pmatrix} D & 0 \\ 0 & 0 \end{pmatrix} P^T,$$

where  $D$  is a  $k$  by  $k$  diagonal matrix with non-zero diagonal elements,  $k$  being the rank of  $R$  and  $w^{\frac{1}{2}} X$ .

This gives the solution

$$\hat{\beta} = P_1 D^{-1} \begin{pmatrix} Q_* & 0 \\ 0 & I \end{pmatrix} Q^T w^{\frac{1}{2}} z$$

$P_1$  being the first  $k$  columns of  $P$ , i.e.,  $P = (P_1 P_0)$ .

The iterations are continued until there is only a small change in the residual sum of squares.

The initial values for the algorithm are obtained by taking

$$\hat{\eta} = g(y)$$

The fit of the model can be assessed by examining and testing the residual sum of squares, in particular comparing the difference in residual sums of squares between nested models, i.e., when one model is a sub-model of the other.

Let  $RSS_f$  be the residual sum of squares for the full model with degrees of freedom  $\nu_f$  and let  $RSS_s$  be the residual sum of squares for the sub-model with degrees of freedom  $\nu_s$  then:

$$F = \frac{(RSS_s - RSS_f)/(\nu_s - \nu_f)}{RSS_f/\nu_f},$$

has, approximately, a  $F$ -distribution with  $(\nu_s - \nu_f)$ ,  $\nu_f$  degrees of freedom.

The parameter estimates,  $\hat{\beta}$ , are asymptotically Normally distributed with variance-covariance matrix:

$$C = R^{-1} R^{-1T} \text{ in the full rank case, otherwise} \\ C = P_1 D^{-2} P_1^T$$

The residuals and influence statistics can also be examined.

The estimated linear predictor  $\hat{\eta} = X\hat{\beta}$ , can be written as  $Hw^{\frac{1}{2}}z$  for an  $n$  by  $n$  matrix  $H$ . The  $i$ th diagonal elements of  $H$ ,  $h_i$ , give a measure of the influence of the  $i$ th values of the independent variables on the fitted regression model. These are sometimes known as leverages.

The fitted values are given by  $\hat{\mu} = g^{-1}(\hat{\eta})$ .

nag\_glm\_normal also computes the residuals,  $r$ :

$$r_i = y_i - \hat{\mu}_i$$

An option allows prior weights,  $\omega_i$  to be used, this gives a model with:

$$\sigma_i^2 = \frac{\sigma^2}{\omega_i}.$$

In many linear regression models the first term is taken as a mean term or an intercept, i.e.,  $x_{i,1} = 1$ , for  $i = 1, 2, \dots, n$ ; this is provided as an option.

Often only some of the possible independent variables are included in a model, the facility to select variables to be included in the model is provided.

If part of the linear predictor can be represented by a variable with a known coefficient, then this can be included in the model by using an offset,  $o$ :

$$\eta = o + \sum \beta_j x_j.$$

If the model is not of full rank the solution given will be only one of the possible solutions. Other estimates may be obtained by applying constraints to the parameters. These solutions can be obtained by using `nag_glm_tran_model` (g02gkc) after using `nag_glm_normal`. Only certain linear combinations of the parameters will have unique estimates; these are known as estimable functions and can be estimated and tested using `nag_glm_est_func` (g02gnc).

Details of the SVD, are made available, in the form of the matrix  $P^*$ :

$$P^* = \begin{pmatrix} D^{-1}P_1^T \\ P_0^T \end{pmatrix}.$$

#### 4. Parameters

##### link

Input: indicates which link function is to be used.

If **link** = **Nag\_Expo**, then an exponent link is used.

If **link** = **Nag\_Iden**, then an identity link is used. The user is advised not to use `nag_glm_normal` with an identity link as `nag_regsn_mult_linear` (g02dac) provides a more efficient way of fitting such a model.

If **link** = **Nag\_Log**, then a log link is used.

If **link** = **Nag\_Sqrt**, then a square root link is used.

If **link** = **Nag\_Reci**, then a reciprocal link is used.

Constraint: **link** = **Nag\_Expo**, **Nag\_Iden**, **Nag\_Log**, **Nag\_Sqrt** or **Nag\_Reci**.

##### mean

Input: indicates if a mean term is to be included.

If **mean** = **Nag\_MeanInclude**, a mean term, (intercept), will be included in the model.

If **mean** = **Nag\_MeanZero**, the model will pass through the origin, zero point.

Constraint: **mean** = **Nag\_MeanInclude** or **Nag\_MeanZero**.

##### n

Input: the number of observations,  $n$ .

Constraint:  $n \geq 2$ .

##### x[n][tdx]

Input:  $x[i-1][j-1]$  must contain the  $i$ th observation for the  $j$ th independent variable, for  $i = 1, 2, \dots, n$ ;  $j = 1, 2, \dots, \mathbf{m}$ .

##### tdx

Input: the second dimension of the array  $\mathbf{x}$  as declared in the function from which `nag_glm_normal` is called.

Constraint:  $\mathbf{tdx} \geq \mathbf{m}$ .

##### m

Input: the total number of independent variables.

Constraint:  $\mathbf{m} \geq 1$ .

##### sx[m]

Input: indicates which independent variables are to be included in the model. If  $sx[j-1] > 0$ , then the variable contained in the  $j$ th column of  $\mathbf{x}$  is included in the regression model.

Constraints:  $sx[j-1] \geq 0$ , for  $j = 1, 2, \dots, \mathbf{m}$ .

if **mean** = **Nag\_MeanInclude**, then exactly  $\mathbf{ip} - 1$  values of  $\mathbf{sx}$  must be  $> 0$ .

if **mean** = **Nag\_MeanZero**, then exactly  $\mathbf{ip}$  values of  $\mathbf{sx}$  must be  $> 0$ .

**ip**

Input: the number  $p$  of independent variables in the model, including the mean or intercept if present.

Constraint: **ip** > 0.

**y[n]**

Input: observations on the dependent variable,  $y_i$ , for  $i = 1, 2, \dots, n$ .

**wt[n]**

Input: if weighted estimates are required then **wt** must contain the weights to be used with the model,  $\omega_i$ . Otherwise **wt** must be supplied as the null pointer, (double \*)0.

If **wt**[ $i - 1$ ] = 0.0, then the  $i$ th observation is not included in the model, in which case the effective number of observations is the number of observations with positive weights.

If **wt** = null pointer, then the effective number of observations is  $n$ .

Constraint: **wt** = null pointer or **wt**[ $i - 1$ ]  $\geq$  0.0, for  $i = 1, 2, \dots, n$ .

**offset[n]**

Input: if an offset is required then **offset** must contain the values of the offset  $o$ . Otherwise **offset** must be supplied as the null pointer, (double \*)0.

**scale**

Input: indicates the scale parameter for the model,  $\sigma^2$ .

If **scale** = 0.0, then the scale parameter is estimated using the residual mean square.

Output: if on input **scale** = 0.0, then **scale** contains the estimated value of the scale parameter,  $\hat{\sigma}^2$ . If on input **scale**  $\neq$  0.0, then **scale** is unchanged on exit.

Constraint: **scale**  $\geq$  0.0.

**ex\_power**

Input: if **link** = **Nag\_Expo** then **ex\_power** must contain the power  $a$  of the exponential.

If **link**  $\neq$  **Nag\_Expo**, **ex\_power** is not referenced.

Constraint: If **link** = **Nag\_Expo**, **ex\_power**  $\neq$  0.0.

**rss**

Output: the residual sum of squares for the fitted model.

**df**

Output: the degrees of freedom associated with the residual sum of squares for the fitted model.

**b[ip]**

Output: **b**[ $i - 1$ ],  $i = 1, 2, \dots, \mathbf{ip}$  contains the estimates of the parameters of the generalized linear model,  $\hat{\beta}$ .

If **mean** = **Nag\_MeanInclude**, then **b**[0] will contain the estimate of the mean parameter and **b**[ $i$ ] will contain the coefficient of the variable contained in column  $j$  of **x**, where **sx**[ $j - 1$ ] is the  $i$ th positive value in the array **sx**.

If **mean** = **Nag\_MeanZero**, then **b**[ $i - 1$ ] will contain the coefficient of the variable contained in column  $j$  of **x**, where **sx**[ $j - 1$ ] is the  $i$ th positive value in the array **sx**.

**rank**

Output: the rank of the independent variables.

If the model is of full rank, then **rank** = **ip**.

If the model is not of full rank, then **rank** is an estimate of the rank of the independent variables. **rank** is calculated as the number of singular values greater than **eps**  $\times$  (largest singular value). It is possible for the SVD to be carried out but **rank** to be returned as **ip**.

**se[ip]**

Output: the standard errors of the linear parameters.

**se**[ $i - 1$ ] contains the standard error of the parameter estimate in **b**[ $i - 1$ ], for  $i = 1, 2, \dots, \mathbf{ip}$ .

**cov[ip\*(ip+1)/2]**

Output: the **ip**  $\times$  (**ip** + 1)/2 elements of **cov** contain the upper triangular part of the variance-covariance matrix of the **ip** parameter estimates given in **b**. They are stored packed by column, i.e., the covariance between the parameter estimate given in **b**[ $i$ ] and the parameter estimate given in **b**[ $j$ ],  $j \geq i$ , is stored in **cov**[ $j(j + 1)/2 + i$ ], for  $i = 0, 1, \dots, \mathbf{ip} - 1$  and  $j = i, i + 1, \dots, \mathbf{ip} - 1$ .

**v[n][tdv]**

Output: auxiliary information on the fitted model.

$\mathbf{v}[i-1][0]$ , contains the linear predictor value,  $\eta_i$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][1]$ , contains the fitted value,  $\hat{\mu}_i$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][2]$ , is only included for consistency with other functions.  $\mathbf{v}[i-1][2] = 1.0$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][3]$ , contains the working weight,  $w_i$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][4]$ , contains the standardised residual,  $r_i$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][5]$ , contains the leverage,  $h_i$ , for  $i = 1, 2, \dots, n$ .

$\mathbf{v}[i-1][j-1]$ , for  $j = 7, \dots, \mathbf{ip}+6$ , contains the results of the *QR* decomposition or the singular value decomposition.

If the model is not of full rank, i.e., **rank** < **ip**, then the first **ip** rows of columns 7 to **ip**+6 contain the *P*\* matrix.

**tdv**

Input: the second dimension of the array **v** as declared in the function from which `nag_glm_normal` is called.

Constraint: **tdv**  $\geq$  **ip**+6.

**tol**

Input: indicates the accuracy required for the fit of the model.

The iterative weighted least-squares procedure is deemed to have converged if the absolute change in deviance between interactions is less than **tol**  $\times$  (1.0+current residual sum of squares). This is approximately an absolute precision if the residual sum of squares is small and a relative precision if the residual sum of squares is large.

If  $0.0 \leq \mathbf{tol} < \mathbf{machine\ precision}$ , then the function will use  $10 \times \mathbf{machine\ precision}$ .

Constraint: **tol**  $\geq$  0.0.

**max\_iter**

Input: the maximum number of iterations for the iterative weighted least-squares.

If **max\_iter** = 0, then a default value of 10 is used.

Constraint: **max\_iter**  $\geq$  0.

**print\_iter**

Input: indicates if the printing of information on the iterations is required and the rate at which printing is produced. The following values are available.

If **print\_iter**  $\leq$  0, then there is no printing.

If **print\_iter** > 0, then the following items are printed every **print\_iter** iterations:

- (i) the deviance,
- (ii) the current estimates, and
- (iii) if the weighted least-squares equations are singular then this is indicated.

**outfile**

Input: a null terminated character string giving the name of the file to which results should be printed. If **outfile** = **NULL** or an empty string then the **stdout** stream is used. Note that the file will be opened in the append mode.

**eps**

Input: the value of **eps** is used to decide if the independent variables are of full rank and, if not, what the rank of the independent variables is. The smaller the value of **eps** the stricter the criterion for selecting the singular value decomposition.

If  $0.0 \leq \mathbf{eps} < \mathbf{machine\ precision}$ , then the function will use **machine precision** instead.

Constraint: **eps**  $\geq$  0.0.

**fail**

The NAG error parameter, see the Essential Introduction to the NAG C Library.

For this function the values of output parameters may be useful even if **fail.code**  $\neq$  **NE\_NOERROR** on exit. Users are therefore advised to supply the **fail** parameter and set **fail.print** = **TRUE**.

## 5. Error Indications and Warnings

**NE\_BAD\_PARAM**

On entry, parameter **link** had an illegal value.  
 On entry, parameter **mean** had an illegal value.

**NE\_INT\_ARG\_LT**

On entry, **n** must not be less than 2: **n** =  $\langle value \rangle$ .  
 On entry, **m** must not be less than 1: **m** =  $\langle value \rangle$ .  
 On entry, **ip** must not be less than 1: **ip** =  $\langle value \rangle$ .  
 On entry, **max\_iter** must not be less than 0: **max\_iter** =  $\langle value \rangle$ .  
 On entry, **sx**[ $\langle value \rangle$ ] must not be less than 0: **sx**[ $\langle value \rangle$ ] =  $\langle value \rangle$ .

**NE\_REAL\_ARG\_LT**

On entry, **scale** must not be less than 0.0: **scale** =  $\langle value \rangle$ .  
 On entry, **tol** must not be less than 0.0: **tol** =  $\langle value \rangle$ .  
 On entry, **eps** must not be less than 0.0: **eps** =  $\langle value \rangle$ .  
 On entry, **wt**[ $\langle value \rangle$ ] must not be less than 0.0: **wt**[ $\langle value \rangle$ ] =  $\langle value \rangle$ .

**NE\_2\_INT\_ARG\_LT**

On entry, **tdx** =  $\langle value \rangle$  while **m** =  $\langle value \rangle$ . These parameters must satisfy **tdx**  $\geq$  **m**.  
 On entry, **tdv** =  $\langle value \rangle$  while **ip** =  $\langle value \rangle$ . These parameters must satisfy **tdv**  $\geq$  **ip**+6.

**NE\_REAL\_ENUM\_ARG\_CONS**

On entry, **ex\_power** = 0.0 , **link** = **Nag\_Expo**.  
 These parameters must satisfy **link** == **Nag\_Expo** && **ex\_power**  $\neq$  0.0.

**NE\_IP\_INCOMP\_SX**

Parameter **ip** is incompatible with parameters **mean** and **sx**.

**NE\_IP\_GT\_OBSERV**

Parameter **ip** is greater than the effective number of observations.

**NE\_VALUE\_AT\_BOUNDARY\_A**

A fitted value is at a boundary. This will only occur with **link** = **Nag\_Expo**, **Nag\_Log** or **Nag\_Reci**. This may occur if there are small values of  $y$  and the model is not suitable for the data. The model should be reformulated with, perhaps, some observations dropped.

**NE\_SVD\_NOT\_CONV**

The singular value decomposition has failed to converge.

**NE\_LSQ\_ITER\_NOT\_CONV**

The iterative weighted least-squares has failed to converge in **max\_iter** =  $\langle value \rangle$  iterations.  
 The value of **max\_iter** could be increased but it may be advantageous to examine the convergence using the **print\_iter** option. This may indicate that the convergence is slow because the solution is at a boundary in which case it may be better to reformulate the model.

**NE\_RANK\_CHANGED**

The rank of the model has changed during the weighted least-squares iterations. The estimate for  $\beta$  returned may be reasonable, but the user should check how the deviance has changed during iterations.

**NE\_ZERO\_DOF\_ERROR**

The degrees of freedom for error are 0. A saturated model has been fitted.

**NE\_NOT\_APPEND\_FILE**

Cannot open file  $\langle string \rangle$  for appending.

**NE\_NOT\_CLOSE\_FILE**

Cannot close file  $\langle string \rangle$ .

**NE\_ALLOC\_FAIL**

Memory allocation failed.

## 6. Further Comments

### 6.1. Accuracy

The accuracy is determined by **tol** as described in Section 4. As the residual sum of squares is a function of  $\mu^2$  the accuracy of the  $\hat{\beta}$ 's will depend on the link used and may be of the order  $\sqrt{\text{tol}}$ .

### 6.2. References

Cook R D and Weisberg S (1982) *Residuals and Influence in Regression*. Chapman and Hall.  
McCullagh P and Nelder J A (1983) *Generalized Linear Models* Chapman and Hall.

## 7. See Also

nag\_regsn\_mult.linear (g02dac)  
nag\_glm\_binomial (g02gbc)  
nag\_glm\_poisson (g02gcc)  
nag\_glm\_gamma (g02gdc)  
nag\_glm\_tran\_model (g02gkc)  
nag\_glm\_est\_func (g02gnc)

## 8. Example

The model:

$$y = \frac{1}{\beta_1 + \beta_2 x} + \epsilon$$

for a sample of 5 observations.

### 8.1. Program Text

```

/* nag_glm_normal(g02gac) Example Program.
 *
 * Copyright 1996 Numerical Algorithms Group.
 *
 * Mark 4, 1996.
 *
 */

#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <ctype.h>
#include <nagg02.h>

#ifdef NAG_PROTO
static void set_enum(char linkc, Nag_Link *link, char meanc,
                    Nag_IncludeMean *mean);
#else
static void set_enum();
#endif

#define NMAX 5
#define MMAX 2
#define TDX MMAX
#define TDV MMAX+6

main()
{
    char linkc, meanc, weightc;
    Nag_Link link;
    Nag_IncludeMean mean;
    Integer i, j, m, n, ip;
    Integer max_iter, print_iter, rank;
    double ex_power, scale, tol, eps, rss, df;
    Integer sx[MMAX];
    double b[MMAX], v[NMAX][TDV], wt[NMAX], x[NMAX][MMAX],

```

```

y[NMAX], se[MMAX], cov[MMAX*(MMAX+1)/2];
double *wtptr, *offsetptr=(double *)0;
static NagError fail;

Vprintf("g02gac Example Program Results\n");
/* Skip heading in data file */
Vscanf("%*[^\\n]");
Vscanf(" %c %c %c %ld %ld %ld %lf", &linkc, &meanc, &weightc, &n,
        &m, &print_iter, &scale);

/* Check and set enum control parameters */
set_enum(linkc, &link, meanc, &mean);
if (n<=NMAX && m<MMAX)
{
    if (toupper(weightc)=='W')
    {
        wtptr = wt;
        for (i=0; i<n; i++)
        {
            for (j=0; j<m; j++)
                Vscanf("%lf", &x[i][j]);
            Vscanf("%lf%lf", &y[i], &wt[i]);
        }
    }
    else
    {
        wtptr = (double *)0;
        for (i=0; i<n; i++)
        {
            for (j=0; j<m; j++)
                Vscanf("%lf", &x[i][j]);
            Vscanf("%lf", &y[i]);
        }
    }
    for (j=0; j<m; j++)
        Vscanf("%ld", &sx[j]);

    /* Calculate ip */
    ip = 0;
    for (j=0; j<m; j++)
        if (sx[j]>0) ip += 1;
    if (mean == Nag_MeanInclude)
        ip += 1;
    if (link == Nag_Expo)
        Vscanf("%lf", &ex_power);
    else
        ex_power = 0.0;

    /* Set other control parameters */
    max_iter = 10;
    tol = 5e-5;
    eps = 1e-6;

    g02gac(link, mean, n, (double *)x, (Integer)TDX, m,
           sx, ip, y, wtptr, offsetptr, &scale, ex_power, &rss, &df, b, &rank,
           se, cov, (double *)v, (Integer)TDV, tol, max_iter,
           print_iter, "", eps, NAGERR_DEFAULT);

    if (fail.code == NE_NOERROR || fail.code == NE_LSQ_ITER_NOT_CONV ||
        fail.code == NE_RANK_CHANGED || fail.code == NE_ZERO_DOF_ERROR)
    {
        Vprintf("\nResidual sum of squares = %12.4e\n", rss);
        Vprintf("Degrees of freedom = %3.1f\n\n", df);
        Vprintf("      Estimate      Standard error\n\n");
        for (i=0; i<ip; i++)
            Vprintf("%14.4f%14.4f\n", b[i], se[i]);
        Vprintf("\n");
        Vprintf("      y      fitted value      Residual      Leverage\n\n");
        for (i = 0; i < n; ++i)
        {

```



```

                Vprintf("%7.1f%10.2f%12.4f%10.3f\n", y[i], v[i][1], v[i][4],
                        v[i][5]);
            }
        }
    else
    {
        Vprintf("%s\n", fail.message);
        exit(EXIT_FAILURE);
    }
}
else
{
    Vfprintf(stderr, "One or both of m and n are out of range:\n
m = %-3ld while n = %-3ld\n", m, n);
    exit(EXIT_FAILURE);
}
exit(EXIT_SUCCESS);
}

#ifdef NAG_PROTO
static void set_enum(char linkc, Nag_Link *link, char meanc,
                    Nag_IncludeMean *mean)
#else
static void set_enum(linkc, link, meanc, mean)
char linkc;
Nag_Link *link;
char meanc;
Nag_IncludeMean *mean;
#endif
{
    if (toupper(linkc) == 'E' || toupper(linkc) == 'I' || toupper(linkc) == 'L'
        || toupper(linkc) == 'S' || toupper(linkc) == 'R')
    {
        switch (toupper(linkc))
        {
            case ('E'):
                *link = Nag_Expo;
                break;
            case ('I'):
                *link = Nag_Iden;
                break;
            case ('L'):
                *link = Nag_Log;
                break;
            case ('S'):
                *link = Nag_Sqrt;
                break;
            case ('R'):
                *link = Nag_Reci;
                break;
            default:
                Vfprintf(stderr, "The parameter link has an invalid value: link = %c\n",
                        linkc);
                exit(EXIT_FAILURE);
        }
    }
    if (toupper(meanc) == 'M')
        *mean = Nag_MeanInclude;
    else if (toupper(meanc) == 'Z')
        *mean = Nag_MeanZero;
    else
    {
        Vfprintf(stderr, "The parameter mean has an invalid value: mean = %c\n",
                meanc);
        exit(EXIT_FAILURE);
    }
    return;
}
}

```

**8.2. Program Data**

```

g02gac Example Program Data
r   m   n   5 1 0 0.0
1.0 25.0
2.0 10.0
3.0  6.0
4.0  4.0
5.0  3.0
1

```

**8.3. Program Results**

```

g02gac Example Program Results

```

```

Residual sum of squares = 3.8717e-01
Degrees of freedom = 3.0

```

	Estimate	Standard error		
	-0.0239	0.0028		
	0.0638	0.0026		
y	fitted value	Residual	Leverage	
25.0	25.04	-0.0387	0.995	
10.0	9.64	0.3613	0.458	
6.0	5.97	0.0320	0.268	
4.0	4.32	-0.3221	0.167	
3.0	3.39	-0.3878	0.112	

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